

Rolando Grave de Peralta Menendez
Sara González Andino · Lucas Perez · Pierre W. Ferrez
José del R. Millán

Non-invasive estimation of local field potentials for neuroprosthesis control

Received: 8 October 2004 / Revised: 9 December 2004 / Accepted: 13 December 2004 / Published online: 18 January 2005
© Marta Olivetti Belardinelli and Springer-Verlag 2005

Abstract Recent experiments have shown the possibility of using the brain electrical activity to directly control the movement of robots or prosthetic devices in real time. Such neuroprostheses can be invasive or non-invasive, depending on how the brain signals are recorded. In principle, invasive approaches will provide a more natural and flexible control of neuroprostheses, but their use in humans is debatable given the inherent medical risks. Non-invasive approaches mainly use scalp electroencephalogram (EEG) signals and their main disadvantage is that these signals represent the noisy spatiotemporal overlapping of activity arising from very diverse brain regions, i.e., a single scalp electrode picks up and mixes the temporal activity of myriads of neurons at very different brain areas. In order to combine the benefits of both approaches, we propose to rely on the non-invasive estimation of local field potentials (LFP) in the whole human brain from the scalp measured EEG data using a recently developed inverse solution (ELECTRA) to the EEG inverse problem. The goal of a linear inverse procedure is to de-convolve or un-mix the scalp signals attributing to each brain area its own temporal activity. To illustrate the advantage of this approach we compare, using an identical set of spectral features, classification of rapid voluntary finger self-tapping with left and right hands based on scalp EEG and non-invasively estimated LFP on two subjects using a different number of electrodes.

Keywords Non-invasive neuroprosthesis · Electroencephalogram · Local field potentials · Inverse solutions

Introduction

Recent experiments have shown the possibility of using the brain electrical activity to directly control the movement of robots or prosthetic devices in real time (Wessberg et al. 2000; Pfurtscheller and Neuper 2001; Meeker et al. 2002; Serruya et al. 2002; Taylor et al. 2002; Carmena et al. 2003; Mehring et al. 2003; Millán et al. 2004). This kind of brain-controlled assistive system is a natural way to augment human capabilities by providing a new interaction link with the outside world. As such, it is particularly relevant as an aid for paralyzed humans, although it also opens up new possibilities in human-robot interaction for able-bodied people.

Initial demonstrations of the feasibility of controlling complex neuroprostheses have relied on intracranial electrodes implanted in the brain of monkeys (Wessberg et al. 2000; Meeker et al. 2002; Serruya et al. 2002; Taylor et al. 2002; Carmena et al. 2003; Mehring et al. 2003). In these experiments, one or more array of microelectrodes records the extracellular activity of single neurons (their spiking rate) in different areas of the cortex related to planning and execution of movements—motor, premotor and posterior parietal cortex. Then, from the real-time analysis of the activity of the neuronal population, it has been possible to predict either the animal's movement intention (Meeker et al. 2002; Mehring et al. 2003) or the monkey's hand trajectory (Wessberg et al. 2000; Taylor et al. 2002; Carmena et al. 2003), and to drive a computer cursor to desired targets (Serruya et al. 2002; Taylor et al. 2002). The motivation for these invasive approaches is that it has been widely shown that motor parameters related to hand and arm movements are encoded in a distributed and redundant way by ensembles of neurons in the

Communicated by Irene Ruspantini and Niels Birbaumer

R. Grave de Peralta Menendez (✉) · S. González Andino
Electrical Neuroimaging Group, Human Brain Mapping
Laboratory, Neurology Department, Geneva University Hospital,
1211 Geneva, Switzerland
E-mail: Rolando.Grave@hcuge.ch
Tel.: +41-22-3728295
Fax: +41-22-3728358

L. Perez · P. W. Ferrez · J. R. Millán
IDIAP Research Institute, 1920 Martigny, Switzerland

motor system of the brain (for a review see Schwartz et al. 2001).

For humans, however, non-invasive methods based on electroencephalogram (EEG) signals are preferable because of ethical concerns and medical risks. The main source of the EEG—the brain electrical activity recorded from electrodes placed over the scalp—is the synchronous activity of thousands of cortical neurons. Thus, EEG signals suffer from a reduced spatial resolution and increased noise due to measurements on the scalp. As a consequence, current EEG-based brain-actuated devices are limited by a low channel capacity and are considered too slow for controlling rapid and complex sequences of movements. So far control tasks based on human EEG have been limited to simple exercises such as moving a computer cursor to the corners of the screen (Wolpaw and McFarland 1994) or opening a hand orthosis (Pfurtscheller and Neuper 2001). However, recently, Millán et al. (2004) have shown for the first time that asynchronous analysis of EEG signals is sufficient for humans to continuously control a mobile robot. Two human subjects learned to mentally drive the robot between rooms in a house-like environment using an EEG-based brain interface that recognized three mental states. Furthermore, mental control was only marginally worse than manual control on the same task. A key element of this brain-actuated robot is a suitable combination of intelligent robotics, asynchronous EEG analysis and machine learning that only requires the user to deliver high-level commands, which the robot performs autonomously, at any time¹.

Despite this latter demonstration of the feasibility of EEG-based neuroprostheses, it is still believed that only invasive approaches will provide natural and flexible control of robots (Nicolelis 2001; Donoghue 2002). The rationale is that surgically implanted arrays of electrodes will be required to properly record the brain signals because the non-invasive scalp recordings with the EEG lack spatial resolution. However, recent advances in EEG analysis techniques have shown that the sources of the electric activity in the brain can be estimated from the surface signals with high spatial accuracy. We believe that such EEG source analysis techniques overcome the lack of spatial resolution and may lead to surface EEG-based neuroprostheses that parallel invasive ones.

The basic question addressed in this paper is the feasibility of non-invasive brain interfaces to reproduce the prediction properties of the invasive systems evaluated in animals while suppressing their risks. Therefore, we propose the non-invasive estimation of local field potentials (LFP) in the whole human brain from the

scalp-measured EEG data using recently developed distributed linear inverse solution termed ELECTRA (Grave de Peralta Menendez et al. 2000). The use of linear inversion procedures yields an on-line implementation of the method, a key aspect for real-time applications.

The development of a brain interface based on ELECTRA, i.e., non-invasive estimates of LFP, allows one to apply methods identical to those used for EEG-based brain interfaces but with the advantage of targeting the activity in specific brain areas. In this respect, our approach aims to parallel the invasive approaches described before that directly feeds intracranial signals into the classification stage of the brain interface, except that we calculate these intracranial signals from the surface EEG data. An additional advantage of our approach over scalp EEG is that the latter represents the noisy spatiotemporal overlapping of activity arising from very diverse brain regions, i.e., a single scalp electrode picks up and mixes the temporal activity of myriads of neurons at very different brain areas. Consequently, temporal and spectral features, which are probably specific to different parallel processes arising at different brain areas, are intermixed on the same recording. This certainly complicates the classification task by misleading even the most sophisticated analysis methods. For example, an electrode placed on the frontal midline picks up and mixes activity related to different motor areas known to have different functional roles such as the primary motor cortex, supplementary motor areas, anterior cingulate cortex, and motor cingulate areas.

On the other hand, the proposed approach bears two main advantages over invasive approaches. First, it avoids any ethical concern and the medical risks associated with intracranial electrocorticographic recordings in humans. Second, the quality of the signals directly recorded on the brain deteriorates over time, requiring new surgical interventions and implants in order to keep the functionality of the device.

The feasibility of this non-invasive LFP approach is shown here in the analysis of single trials recorded during self-paced finger tapping with right and left hands. To illustrate the generalization of our approach and the influence of the number of electrodes, we report results obtained with two normal volunteers using 111 and 32 electrodes, respectively. The capability to predict and differentiate the laterality of the movement using scalp EEG is compared with that of LFP estimated using ELECTRA inverse solution.

Methods

Data recording

Two healthy right-handed young subjects (males, 30 years and 32 years) completed a self-paced finger-tapping task. Subjects were instructed to press at their

¹This is possible because the operation of the brain interface is asynchronous and, unlike synchronous approaches (Wolpaw and McFarland 1994; Birbaumer et al. 1999; Donchin et al. 2000; Roberts and Penny 2000; Pfurtscheller and Neuper 2001), does not require waiting for external cues that arrive at a fixed pace of 4–10 s.

own pace the left mouse button with the index finger of a given hand while fixating a white cross at the middle of the computer screen. The intervals between successive movements were rather stable for the two subjects, namely, around 500 ms and 2,000 ms for subjects A and B, respectively. Subjects performed several sessions of the task with breaks of around 5–10 min in between.

The EEG was recorded at 1,000 Hz from 111 scalp electrodes (Electric Geodesic Inc. system, subject A) and at 512 Hz from 32 scalp electrodes (Biosemi Active Two system, subject B). Head position was stabilized with a head and chin rest. In the first case (i.e., 111 electrodes), off-line processing of the scalp data consisted uniquely in the rejection of bad channels and their interpolation using a simple nearest neighbor's algorithm. This procedure was not necessary with the 32-electrode system. Since digitized electrode positions were not available, we used standard spherical positions and the 10-10 system. These positions were projected onto the scalp of the segmented average MNI brain ².

The pace selected by the subjects allowed for the construction of trials aligned by the response consisting of 400 ms before key press. We recorded 680 trials of the left index tapping and 634 trials of the right index tapping for subject A, while for subject B we recorded 140 left trials and 145 right trials. We did not apply any visual or automatic artifact rejection and so kept all trials for analysis ³.

Local field potentials estimates from scalp EEG recordings

The EEG measures the extracranial electric fields produced by neuronal activity within a living brain. When the positions and orientations of the active neurons in the brain are known, it is possible to calculate the patterns of electric potentials on the surface of the head produced by these sources. This process is called the

²This projection is based on the best-fitting sphere with center and radius selected to fit the scalp region used by the electrodes. This method requires the careful positioning of the electrodes based on anatomical landmarks, i.e., vertex electrode (Cz), middle line, frontal electrodes (Fp) etc. Note that, due to the inaccuracies of boundary detection algorithms, there is no rigid transformation able to “land” a set of electrodes on the scalp detected from the MRI. For this reason, most landing procedures need, at some stage, to project electrode positions on the detected scalp. This procedure has been widely used and tested in clinical studies using standard EEG configurations (e.g., 10-20 and 10-10 systems) where the subject's MRI is not available as well as in the construction of realistic head models for presurgical evaluation of epileptic patients. Still, minor differences between electrode locations might be expected from one session to another. These variations can be considered as noise in the data and its influence can be alleviated with regularization strategies.

³After a visual a posteriori artifact check of the trials, we found no evidence of muscular artifacts that could have contaminated one condition differently from the other.

forward problem. If instead the only available information is the measured pattern of electric potential on the scalp surface, then one is interested in determining the intracranial distribution of neural activity. This is called the inverse problem or the source localization problem, for which there is no unique solution. The only hope is that additional information can be used to constrain the infinite set of possible solutions to a single one. Depending on the additional information, different inverse solutions, i.e., different reconstructions of neural activities with different properties, can be obtained (van Oosterom 1991; Scherg 1994).

Classical constraints used to solve the EEG inverse problem rely on considering the neural generators as current dipoles (Ilmoniemi 1993). In this case, the magnitude to estimate is the dipole model, supposed to represent a current density vector that can be distributed over the whole gray matter mantle or confined to a single point. When the dipole is assumed to be confined to a single or few brain sites, the task is to solve a nonlinear optimization problem aimed to find simultaneously the position and dipolar model of the dipoles (Scherg 1992; Mosher et al. 1999). When the dipoles are distributed over a discrete set of solution points within the brain, the task is to find the magnitude of the dipolar model for each dipole leading to an underdetermined inverse problem which is usually solved by adding linear constraints such as minimum norm, etc. (Hamalainen and Ilmoniemi 1994; Grave de Peralta Menendez and Gonzalez Andino 1998). In both approaches, single dipoles or distributed dipoles, the magnitude to be estimated is a vector field commonly termed the current density vector. However, in the second approach that considers distributed models, the values of the current density vector are obtained for the whole gray matter akin to the tomographic images produced by other modalities of functional neuroimaging (fMRI, PET, or SPECT), but with temporal resolution in the order of milliseconds.

A change in the formulation of the EEG inverse problem takes place when the fact that neurophysiological currents are ohmic and can therefore be expressed as gradients of potential fields is included as constraint in the formalism of the problem (Grave de Peralta Menendez et al. 2000). With this neurophysiological constraint, we can reformulate the EEG inverse problem in more restrictive terms, providing the basis for the non-invasive estimation of intracranial LFP (a scalar field) instead of the current density vector (a 3D vector field) (Grave de Peralta Menendez et al. 2004). This solution is termed ELECTRA.

ELECTRA can be intuitively described as the non-invasive estimation of LFP by means of virtual intracranial electrodes. The advantages of this method are:

1. Mathematical simplicity and computational efficiency compared to models based on current density estimation, since the number of unknowns estimated by the inverse model is threefold fewer, i.e., the unknowns decrease from a vector field to a scalar field.

2. Contrary to dipolar models, distributed linear solutions provide simultaneous temporal estimates for all brain areas not being confined to a few sites.
3. The temporal reconstructions provided by linear distributed inverse solutions are better than those of discrete spatiotemporal models or L1-based reconstructions (Liu et al. 1998). A few comparisons with intracranial data are also extremely appealing, suggesting systematically that temporal reconstructions of the generators are more reliable than their spatial counterparts.
4. Since these are linear methods, computation of the intracranial estimates reduces to a simple inverse matrix by vector product, which warrants efficient on-line implementation.

The analysis that follows relies on the estimation for each single trial of the 3D distribution of the LFP using ELECTRA source model. The head model, relating intracranial sources to scalp measurements, was derived from the Montreal Neurological Institute average brain. The LFP were then estimated at 4,024 pixels distributed on a 6-mm regular grid restricted to the gray matter of the brain model.

Statistical classifier

The different mental tasks are recognized by a Gaussian classifier trained to classify samples (single trials) as class “left” or “right” (Millán et al. 2002b, 2004). The output of this statistical classifier is an estimation of the posterior class probability distribution for a sample; i.e., the probability that a given single trial belongs either to class “left” or class “right”.

In this statistical classifier, every Gaussian unit represents a prototype of one of the mental tasks (or classes) to be recognized. We use several prototypes per mental task. We assume that the class-conditional probability density function of class C_k is a superposition of N_k Gaussians (or prototypes) and that classes have equal prior probabilities. In our case, all the classes have the same number of prototypes. In addition, we assume that all prototypes have an equal weight of $1/N_k$. The challenge is to find the appropriate position of the Gaussian prototype as well as an appropriate variance.

Usually, each prototype of a given class C_k has its own covariance matrix \sum_k^i . In our case, in order to reduce the number of parameters, we restrict our model to a diagonal covariance matrix \hat{O}_k that is common to all the prototypes of the class C_k .

To initialize the center of the prototypes, μ_k^i , of the class C_k we run a clustering algorithm—typically, self-organizing maps (Kohonen 1997). We then initialize the diagonal covariance matrix by setting

$$(\Sigma_k)_{mm} = \frac{1}{|S_k|} \sum_{n \in S_k} (x^n - \mu_k^{i^*(n)})^2 \quad (1)$$

where S_k denotes the set of indexes of samples belonging to the class C_k , $|S_k|$ is the cardinality of this set, $i^*(n)$ is the nearest prototype of this class to the sample x^n , and $\mu_k^{i^*(n)}$ is its center. The index m denotes the element of a vector, and mm the diagonal element of a matrix.

During learning, we improve these initial estimations iteratively by stochastic gradient descent so as to minimize the mean square error $E = \frac{1}{2} \sum_j (y_j - t_j)^2$ where t_j is the j th component of the target vector in the form *1-of-c*; e.g., the target vector for class “left” is coded as (0,1).

After updating μ_k^i and \sum_k^i for a given training sample, the covariance matrices of all the prototypes of the same class are averaged to obtain the common class covariance matrix \hat{O}_k . This simple operation leads to better performance than if separate covariance matrices are kept for each individual prototype. It is also worth noting that given the relatively low number of parameters of the covariance matrices to be estimated, as compared to when we use the full matrices, usual regularization techniques (e.g., Hastie et al. 2001) do not improve performance. The interpretation of this rule is that, during training, the centers of the Gaussians are pulled towards the samples of the mental task they represent and are pushed away from samples of other task.

Feature extraction

To test the capability of our LFP approach to discriminate between left and right finger movements, we have done a tenfold cross-validation study and also have compared the performance of the LFP-based classifier to an EEG-based classifier.

In the case of using scalp EEG signals, each single trial of 400 ms of raw EEG potentials is first spatially filtered by means of a common average reference method (removal of the average activity over all the electrodes). Spatial filtering yields new potentials that represent better the cortical activity due only to local sources below the electrodes. The superiority of this kind of transformed potentials over raw potentials for the operation of a brain interface has been demonstrated in different studies (e.g., Babiloni et al. 2000). Then the power spectral density (PSD) in the band 8–30 Hz was estimated for the ten channels CPz, Pz, FC3, FC4, C3, C4, CP3, CP4, P3, P4, which cover the motor cortex bilaterally. We have successfully used these PSD features in previous experiments (Millán et al. 2002b, 2004). In particular, we computed the PSD using modern multitaper methods (Thomson 1982). These methods have shown to be particularly well suited for spectral analysis of short segments of noisy data, and have been successfully applied to the analysis of neuronal recordings in behaving animals (e.g., Pesaran et al. 2002). Specifically, the PSD was estimated using seven Slepian data tapers.

In the case of the classifier based on the estimated LFP, we have also computed the PSD in the band

8–30 Hz using multitaper methods with seven Slepian data tapers. The PSD was estimated for each single trial of 400 ms on the 50 most relevant pixels (out of 4,024) as selected by a feature selection algorithm that is a variant of the so-called Relief method (Kira and Rendell 1992). Relief has been successfully applied to the selection of relevant spectral features for the classification of EEG signals (Millán et al. 2002a). Feature selection was only applied to the estimated LFP because of the large number of potential pixels that can be fed to the classifier. In the case of scalp EEG, it has been widely shown that only channels over the motor cortex suffice for good recognition of bimanual movements. Also, feature selection was done on the training set of each cross-validation step.

Results

Table 1 shows the results of this comparative study based, as explained before, on a tenfold cross-validation using the Gaussian classifier. This means that all the available single trials of each class are split in ten different subsets, and then we take nine of them to train the classifier and the remaining for testing the generalization capabilities. This process is repeated ten times to get an average of the performance of the classifier based on PSD features computed either on surface EEG or non-invasive estimates of LFP.

Classification based on surface EEG achieves error rates similar to previous studies (11% on average for the two subjects), and that despite the short time windows used to estimate the PSD, namely 400 ms. In particular, performance is worse for subject A than for subject B (11.6% vs. 10.5%), which illustrates the difficulty of recognizing rapid motor decisions (500 ms tapping pace vs. 2,000 ms) based on short segments of brain electrical activity.

In contrast, the performance of the Gaussian classifier based on non-invasive LFP is extremely good as it only makes 3.7% and 4.9% errors for subjects A and B, respectively. These performances are three- and twofold better than when using surface EEG features, respectively. This clearly shows the advantage of using non-invasive estimations of LFP over surface EEG. This is particularly the case for subject A, for whom we recorded from 111 electrodes. In addition, it is also worth

Table 1 Error rates in the recognition of “left” versus “right” finger movements made by a Gaussian classifier based on PSD features computed either on surface EEG or non-invasive LFP using the multitaper method for subjects A and B. Results are the average of a tenfold cross-validation study

Method	Subject (%)	
	A	B
EEG multitaper	11.6	10.5
LFP multitaper	3.7	4.9

noting that performance is still very good for subject B even if the LFP were estimated from only 32 scalp electrodes.

Regarding the spatial distribution of the pixels selected by the feature selection algorithm, they form clusters located on the frontal cortex with tendency to have the most relevant ones at the dorso-lateral pre-motor cortex and including different frequency values. Altogether, these results suggest that the prediction capabilities of brain interfaces based on non-invasive estimations of LFP might parallel those of invasive approaches.

Discussion

The goal of a linear inverse procedure is to de-convolve or un-mix the scalp signals attributing to each brain area its own temporal activity. By targeting on the particular temporal/spectral features at specific brain areas, we can select a low number of features that capture information related to the state of the individual in a way that is relatively invariant to time. Eventually, this may avoid long training periods and increase the reliability and efficiency of the classifiers. For the case of paralyzed patients the classification stage can be improved by focusing on the specific brain areas known to participate and code the different steps of voluntary or imagined motor action through temporal and spectral features.

Distributed inverse solutions, as any other inverse method, suffer from limitations inherent to the ill-posed nature of the problem. The limitations of these methods have been already described (Grave de Peralta Menendez and Gonzalez Andino 1998) and concern basically: (1) errors on the estimation of the sources’ amplitudes for the instantaneous maps and (2) inherent blurring, i.e., the spatial extent of the actual source is usually overestimated. However, several theoretical and experimental studies showed that spectral and temporal features are quite well preserved by these methods (Grave de Peralta Menendez et al. 2000) that surpass nonlinear and dipolar methods (Liu et al. 1998). The analysis strategy selected in our research plan relies on temporal and spectral features disregarding estimated amplitudes so as to alleviate these limitations.

Finally, since the head model is stable for the same subject over time, the inverse matrix requires to be computed only once for each subject and is invariant over recording sessions. On-line estimation of intracranial field potentials is reduced to a simple inverse-matrix-by-data-product, which yields an on-line implementation, a key aspect for real-time applications. However, despite a careful positioning of the electrodes and the regularization used to deal with the noise associated to electrode misplacement, the estimated activity might still result displaced to a neighbor location out of the strict boundaries defined in the anatomical atlas. This could happen because of the differences between the subject head and the average MNI head model or

due to the differences in electrode locations from one session to another. Based on the results of the extensive studies of presurgical evaluation of epileptic patients, we should expect low errors using realistic head models based on subjects' MRI. However, since presurgical studies barely use more than one EEG recording session, the second source of error requires further study.

Regarding the possibility of using biophysically constrained inverse solutions for the control of neuroprostheses, the results reported in this paper are highly encouraging. They suggest that recognition of motor intents is possible from non-averaged inverse solutions and are even superior to systems based on scalp EEG. This could be the basis of the non-invasive brain-computer interface put forward by Grave de Peralta Menendez et al. (2003) allowing for a real-time anticipation of the direction of the upcoming movements. While such anticipation is possible from invasive recordings from neuronal populations in the motor cortex of monkeys (Carmena et al. 2003) as well as from LFP recorded from the motor cortex of monkeys (Mehring et al. 2003), the possibility of doing the same non-invasively is appealing for its much higher potential with humans. Finally, the use of non-invasive estimations of LFP at specific brain areas allows for the replacement of most of the empirical features used in classical EEG-based brain interfaces by features with a priori established neurophysiological information.

Acknowledgements This work was supported by the Swiss National Science Foundation through the National Center of Competence in Research on "Interactive Multimodal Information Management (IM2)" and also by the Swiss National Science Foundation grant 3152A0-100745/1.

References

- Babiloni F, Cincotti F, Lazzaroni L, Millán J del R, Mouriño J, Varsta M, Heikkinen J, Bianchi L, Marciani MG (2000) Linear classification of low-resolution EEG patterns produced by imagined hand movements. *IEEE Trans Rehab Eng* 8:186–188
- Birbaumer N, Ghanayim N, Hinterberger T, Iversen I, Kotchoubey B, Kübler A, Perlmouter J, Taub E, Flor H (1999) A spelling device for the paralysed. *Nature* 398:297–298
- Carmena JM, Lebedev MA, Crist RE, O'Doherty JE, Santucci DM, Dimitrov DF, Patil PG, Henriquez CS, Nicolelis MAL (2003) Learning to control a brain-machine interface for reaching and grasping by primates. *PLoS Biol* 1:193–208
- Donchin E, Spencer KM, Wijesinghe R (2000) The mental prosthesis: assessing the speed of a P300-based brain-computer interface. *IEEE Trans Rehab Eng* 8:174–179
- Donoghue JP (2002) Connecting cortex to machines: recent advances in brain interfaces. *Nat Neurosci Suppl* 5:1085–1088
- Grave de Peralta R, Gonzalez Andino SL, Millán J del R, Pun T, Michel CM (2003) Direct non-invasive brain computer interfaces. In: 9th International Conference on Functional mapping of the human brain
- Grave de Peralta Menendez R, Gonzalez Andino SL (1998) A critical analysis of linear inverse solutions to the neuroelectromagnetic inverse problem. *IEEE Trans Biomed Eng* 45:440–448
- Grave de Peralta Menendez R, Gonzalez Andino SL, Morand S, Michel CM, Landis T (2000) Imaging the electrical activity of the brain: ELECTRA. *Hum Brain M* 9:1–12
- Grave de Peralta Menendez R, Murray MM, Michel CM, Marzuzzi R, Gonzalez Andino SL (2004) Electrical neuroimaging based on biophysical constraints. *Neuroimage* 21:527–539
- Hamalainen MS, Ilmoniemi RJ (1994) Interpreting magnetic fields of the brain: minimum norm estimates. *Med Biol Eng Comput* 32:35–42
- Hastie T, Tibshirani R, Friedman J (2001) The elements of statistical learning. Springer, Berlin Heidelberg New York
- Ilmoniemi RJ (1993) Models of source currents in the brain. *Brain Topogr* 5:331–336
- Kira K, Rendell LA (1992) The feature selection problem: traditional methods and a new algorithm. In: 9th National Conference on Artificial intelligence, pp 129–134
- Kohonen T (1997) Self-organizing maps, 2nd edn. Springer, Berlin Heidelberg New York
- Liu AK, Belliveau JW, Dale AM (1998) Spatiotemporal imaging of human brain activity using functional MRI constrained magnetoencephalography data: Monte Carlo simulations. *Proc Natl Acad Sci USA* 95:8945–8950
- Meeker D, Cao S, Burdick JW, Andersen RA (2002) Rapid plasticity in the parietal reach region demonstrated with a brain-computer interface. 2002 Abstract Viewer/Planner, Program no 257.7.2002, Society for Neuroscience
- Mehring C, Rickert J, Vaadia E, Cardoso de Oliveira S, Aerten A, Rotter S (2003) Inference of hand movements from local field potentials in the monkey motor cortex. *Nat Neurosci* 6:1253–1254
- Millán J del R, Franzé M, Mouriño J, Cincotti F, Babiloni F (2002a) Relevant EEG features for the classification of spontaneous motor-related tasks. *Biol Cybern* 86:89–95
- Millán J del R, Mouriño J, Franzé M, Cincotti F, Varsta M, Heikkinen J, Babiloni F (2002b) A local neural classifier for the recognition of EEG patterns associated to mental tasks. *IEEE Trans Neural Netw* 13:678–686
- Millán J del R, Renkens F, Mouriño J, Gerstner W (2004) Non-invasive brain-actuated control of a mobile robot by human EEG. *IEEE Trans Biomed Eng* 51:1026–1033
- Mosher JC, Baillet S, Leahy RM (1999) EEG source localization and imaging using multiple signal classification approaches. *J Clin Neurophysiol* 16:225–238
- Nicolelis MAL (2001) Actions from thoughts. *Nature* 409:403–407
- van Oosterom A (1991) History and evolution of methods for solving the inverse problem. *J Clin Neurophysiol* 8:371–380
- Pesaran B, Pezaris JS, Sahani M, Mitra PP, Andersen RA (2002) Temporal structure in neuronal activity during working memory in macaque parietal cortex. *Nat Neurosci* 5:805–811
- Pfurtscheller G, Neuper C (2001) Motor imagery and direct brain-computer communication. *Proc IEEE* 89:1123–1134
- Roberts SJ, Penny WD (2000) Real-time brain-computer interfacing: a preliminary study using Bayesian learning. *Med Biol Eng Comput* 38:56–61
- Scherg M (1992) Functional imaging and localization of electromagnetic brain activity. *Brain Topogr* 5:103–111
- Scherg M (1994) From EEG source localization to source imaging. *Acta Neurol Scand Suppl* 152:29–30
- Schwartz AB, Taylor DM, Helms Tillery SI (2001) Extraction algorithms for cortical control of arm prosthetics. *Curr Opin Neurobiol* 11:701–707
- Serruya MD, Hatsopoulos NG, Paninski L, Fellows MR, Donoghue J (2002) Instant neural control of a movement signal. *Nature* 416:141–142
- Taylor DM, Helms Tillery SI, Schwartz AB (2002) Direct cortical control of 3D neuroprosthetic devices. *Science* 296:1829–1832
- Thomson DJ (1982) Spectrum estimation and harmonic analysis. *Proc IEEE* 70:1055–1096
- Wessberg J, Stambaugh CR, Kralik JD, Beck PD, Laubach M, Chapin JK, Kim J, Biggs SJ, Srinivasan MA, Nicolelis MAL (2000) Real-time prediction of hand trajectory by ensembles of cortical neurons in primates. *Nature* 408:361–365
- Wolpaw JR, McFarland DJ (1994) Multichannel EEG-based brain-computer communication. *Electroencephalogr Clin Neurophysiol* 90:444–449